

## EXPERIMENT 4

## EQUIVALENT CIRCUIT OF A SINGLE PHASE TRANSFORMER

## Objective:

- To perform the no-load (open circuit) and short circuit tests
- To calculate the single phase transformer's equivalent circuit parameters

## Equipment:

- Single phase transformer
- Measurement devices: Ammeter, Voltmeter, Wattmeter

## Procedure:

- Sketch equivalent circuit diagram of a single phase transformer.
- Record nameplate values of the transformer.
- First apply DC test, thus measure primary and secondary winding resistances.
- Apply open circuit test; Measure and record I, V and P values.
- Calculate core resistance and magnetizing reactance values using open circuit measurements.
- Apply short circuit test; Measure and record I, V and P values.
- Calculate equivalent impedance, resistance and reactance first, then determine primary and secondary values.

## Questions:

- Briefly state terms; referred to low-voltage side and referred to high-voltage side.
- If one wants to observe hysteresis loop of a transformer via an oscilloscope, what would be the circuit setup you would propose to her ?
- Convert equivalent circuit referred to secondary.

## EXAMPLE PROBLEM

A 2000-VA 230/115-V transformer has been tested to determine its equivalent circuit. The results of the tests are shown below.

Open-circuit test	Short-circuit test
$V_{OC} = 230 \text{ V}$	$V_{SC} = 13.2 \text{ V}$
$I_{OC} = 0.45 \text{ A}$	$I_{SC} = 6.0 \text{ A}$
$P_{OC} = 30 \text{ W}$	$P_{SC} = 20.1 \text{ W}$

All data given were taken from the primary side of the transformer.

Find the equivalent circuit of this transformer referred to the low-voltage side of the transformer.

(a) OPEN CIRCUIT TEST:

$$|Y_{EX}| = |G_C - jB_M| = \frac{0.45 \text{ A}}{230 \text{ V}} = 0.001957 \text{ S}$$

$$\theta = \cos^{-1} \frac{P_{OC}}{V_{OC} I_{OC}} = \cos^{-1} \frac{30 \text{ W}}{(230 \text{ V})(0.45 \text{ A})} = 73.15^\circ$$

$$Y_{EX} = G_C - jB_M = 0.001957 \angle -73.15^\circ \text{ S} = 0.000567 - j0.001873 \text{ S}$$

$$R_C = \frac{1}{G_C} = 1763 \Omega$$

$$X_M = \frac{1}{B_M} = 534 \Omega$$

SHORT CIRCUIT TEST:

$$|Z_{EQ}| = |R_{EQ} + jX_{EQ}| = \frac{13.2 \text{ V}}{6.0 \text{ A}} = 2.20 \Omega$$

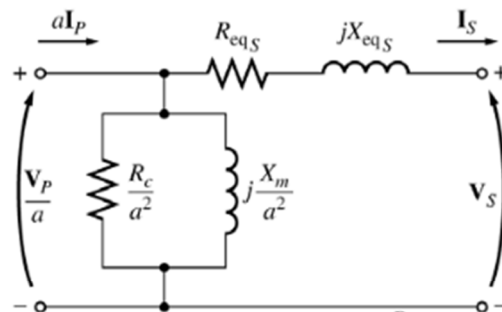
$$\theta = \cos^{-1} \frac{P_{SC}}{V_{SC} I_{SC}} = \cos^{-1} \frac{20.1 \text{ W}}{(13.2 \text{ V})(6 \text{ A})} = 75.3^\circ$$

$$Z_{EQ} = R_{EQ} + jX_{EQ} = 2.20 \angle 75.3^\circ \Omega = 0.558 + j2.128 \Omega$$

$$R_{EQ} = 0.558 \Omega$$

$$X_{EQ} = j2.128 \Omega$$

To convert the equivalent circuit to the secondary side, divide each impedance by the square of the turns ratio ( $a = 230/115 = 2$ ). The resulting equivalent circuit is shown below:



$$(b) \quad R_{eq,S} = \frac{R_p}{a^2} + R_S$$

$$X_{eq,S} = \frac{X_p}{a^2} + X_S$$

$$R_{EQ,S} = 0.140 \Omega$$

$$X_{EQ,S} = j0.532 \Omega$$

$$R_{C,S} = 441 \Omega$$

$$X_{M,S} = 134 \Omega$$