

### CHEMISTRY

The Central Science 8<sup>th</sup> Edition

## Chapter 15 Chemical Equilibrium

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### The Concept of Equilibrium



- Chemical equilibrium is the point at which the concentrations of all species are constant.
- Chemical equilibrium occurs when opposing reactions are proceeding at equal rates.



## The Concept of Equilibrium



- As a system approaches *equilibrium*, both the *forward* and *reverse* reactions are occurring.
- At equilibrium, the forward and reverse reactions are proceeding *at the same rate*.





### A System at Equilibrium

Once equilibrium is achieved, the *amount* of each *reactant* and *product* remains *constant*.





Rate = 
$$k_f$$
 [A]  
Rate =  $k_r$  [B]  
 $PV = nRT$ , so  $M = (n/V) = (P/RT)$   
Rate =  $k_f \frac{P_A}{RT}$ 

## Equilibrium

• In a system at equilibrium, both the forward and reverse reactions are being carried out; as a result, we write its equation with a double arrow

$$N_2O_{4(g)} = 2NO_{2(g)}$$

• Consider

Forward reaction:  $A \rightarrow B$  Rate =  $k_f[A]$ Reverse reaction:  $B \rightarrow A$  Rate =  $k_r[B]$ 

• At equilibrium  $k_f[A] = k_r[B]$ .





• Forward reaction:

 $N_2O_{4(g)} \longrightarrow 2 NO_{2(g)}$ 

- Rate law: Rate =  $k_f [N_2O_4]$
- Reverse reaction:  $2 \operatorname{NO}_{2(g)} \longrightarrow \operatorname{N}_2\operatorname{O}_{4(g)}$
- Rate law:

Rate =  $k_r [NO_2]^2$ 

at equilibrium

 $Rate_{f} = Rate_{r}$  $k_{f} [N_{2}O_{4}] = k_{r} [NO_{2}]^{2}$ 

#### Rewriting this, it becomes



• To generalize this expression, consider the reaction

$$aA + bB \longrightarrow cC + dD$$

• The equilibrium expression for this reaction would be

$$K_c = \frac{[C]^c[D]^d}{[A]^a[B]^b}$$



Because *pressure* is proportional to concentration for *gases* in a *closed system*, the equilibrium expression can also be written

$$K_{p} = \frac{(P_{C})^{c} (P_{D})^{d}}{(P_{A})^{a} (P_{B})^{b}}$$

From the *ideal gas* law we know that

$$P = \frac{n}{V} RT \qquad K_p = K_c (RT)^{\Delta n}$$

 $\Delta n$  = (moles of gaseous product) – (moles of gaseous reactant)

- $K_{eq}$  is based on the molarities of reactants and products at equilibrium.
- As you can see, the ratio of  $[NO_2]^2$  to  $[N_2O_4]$  remains constant at this temperature no matter what the *initial concentrations* of NO<sub>2</sub> and N<sub>2</sub>O<sub>4</sub> are.
- The same equilibrium is established not matter how the reaction is begun.

Experiment	Initial N <sub>2</sub> O <sub>4</sub> Concentration ( <i>M</i> )	Initial NO <sub>2</sub> Concentration ( <i>M</i> )	Equilibrium N <sub>2</sub> O <sub>4</sub> Concentration ( <i>M</i> )	Equilibrium NO <sub>2</sub> Concentration ( <i>M</i> )	K <sub>c</sub>
1	0.0	0.0200	0.00140	0.0172	0.211
2	0.0	0.0300	0.00280	0.0243	0.211
3	0.0	0.0400	0.00452	0.0310	0.213
4	0.0200	0.0	0.00452	0.0310	0.213

## Equilibrium can be reached from either direction



This is the data from the last two trials from the table on the previous slide.

It does not matter whether we start with  $N_2$  and  $H_2$  or whether we start with  $NH_3$ . We will have the same proportions of all three substances at equilibrium.



### What Does the Value of K Mean?



#### (a) K >> 1



 If K >> 1, the reaction is product-favored; product predominates at equilibrium.

 If K << 1, the reaction is reactant-favored; reactant predominates at equilibrium.



$$CO(g) + Cl_2(g) \Longrightarrow COCl_2(g)$$
  $K_c = = \frac{[COCl_2]}{[CO][Cl_2]} = 4.56 \times 10^9$ 



## Manipulating Equilibrium Constants

The equilibrium constant of a reaction in the reverse reaction is the reciprocal of the equilibrium constant of the forward reaction.

$$N_{2}O_{4}(g) = 2 NO_{2}(g) K_{c} = \frac{[NO_{2}]^{2}}{[N_{2}O_{4}]} = 0.212 \text{ at } 100^{\circ}\text{C}$$

$$2 NO_{2}(g) = N_{2}O_{4}(g) K_{c} = \frac{[N_{2}O_{4}]}{[NO_{2}]^{2}} = \frac{1}{0.212}$$



### **Manipulating Equilibrium Constants**

The equilibrium constant of a reaction that has been multiplied by a number is the equilibrium constant raised to a power that is equal to that number.

$$N_2O_4(g) = 2 NO_2(g) K_c = \frac{[NO_2]^2}{[N_2O_4]} = 0.212 \text{ at } 100^{\circ}\text{C}$$

 $2 N_2 O_4 (g) = 4 NO_2 (g) K_c = \frac{[NO_2]^4}{[N_2 O_4]^2} = (0.212)^2 \text{ at } 100^{\circ}\text{C}$ 



### Manipulating Equilibrium Constants

The equilibrium constant for a net reaction made up of two or more steps is the product of the equilibrium constants for the individual steps.

$$2 \operatorname{NOBr}(g) \rightleftharpoons 2 \operatorname{NO}(g) + \operatorname{Br}_2(g) \quad K_c = \frac{[\operatorname{NO}]^2[\operatorname{Br}_2]}{[\operatorname{NOBr}]^2} = 0.014$$
$$\operatorname{Br}_2(g) + \operatorname{Cl}_2(g) \rightleftharpoons 2 \operatorname{BrCl}(g) \qquad K_c = \frac{[\operatorname{BrCl}]^2}{[\operatorname{Br}_2][\operatorname{Cl}_2]} = 7.2$$

The net sum of these two equations is

$$2 \operatorname{NOBr}(g) + \operatorname{Cl}_2(g) \Longrightarrow 2 \operatorname{NO}(g) + 2 \operatorname{BrCl}(g)$$

and the equilibrium-constant expression for the net equation is the product of the expressions for the individual steps:

$$K_c = \frac{[\text{NO}^2][\text{BrCl}]^2}{[\text{NOBr}]^2[\text{Cl}_2]} = \frac{[\text{NO}]^2[\text{Br}_2]}{[\text{NOBr}]^2} \times \frac{[\text{BrCl}]^2}{[\text{Br}_2][\text{Cl}_2]}$$





#### SAMPLE EXERCISE 15.5 Combining Equilibrium Expressions

Given the following information,

$$HF(aq) \Longrightarrow H^{+}(aq) + F^{-}(aq) \qquad K_{c} = 6.8 \times 10^{-4}$$
$$H_{2}C_{2}O_{4}(aq) \Longrightarrow 2 \text{ H}^{+}(aq) + C_{2}O_{4}^{2-}(aq) \qquad K_{c} = 3.8 \times 10^{-6}$$

determine the value of  $K_c$  for the reaction

$$2 \operatorname{HF}(aq) + \operatorname{C}_2\operatorname{O}_4^{2-}(aq) \Longrightarrow 2 \operatorname{F}^-(aq) + \operatorname{H}_2\operatorname{C}_2\operatorname{O}_4(aq)$$





**Solve:** If we multiply the first equation by 2 and make the corresponding change to its equilibrium constant (raising to the power 2), we get

Reversing the second equation and again making the corresponding change to its equilibrium constant (taking the reciprocal) gives

Now we have two equations that sum to give the net equation, and we can multiply the individual  $K_c$ values to get the desired equilibrium constant.

$$2 \text{ HF}(aq) \implies 2 \text{ H}^+(aq) + 2 \text{ F}^-(aq) \quad K_c = (6.8 \times 10^{-4})^2 = 4.6 \times 10^{-4}$$

$$2 H^+(aq) + C_2 O_4^{2-}(aq) \Longrightarrow H_2 C_2 O_4(aq) \quad K_c = \frac{1}{3.8 \times 10^{-6}} = 2.6 \times 10^5$$

$$2 \operatorname{HF}(aq) \rightleftharpoons 2 \operatorname{H}^{+}(aq) + 2 \operatorname{F}^{-}(aq) \qquad K_{c} = 4.6 \times 10^{-7}$$

$$\underline{2 \operatorname{H}^{+}(aq) + \operatorname{C}_{2}\operatorname{O}_{4}^{2^{-}}(aq) \rightleftharpoons \operatorname{H}_{2}\operatorname{C}_{2}\operatorname{O}_{4}(aq)}_{2 \operatorname{HF}(aq) + \operatorname{C}_{2}\operatorname{O}_{4}^{2^{-}}(aq) \rightleftharpoons 2 \operatorname{F}^{-}(aq) + \operatorname{H}_{2}\operatorname{C}_{2}\operatorname{O}_{4}(aq) \qquad K_{c} = (4.6 \times 10^{-7})(2.6 \times 10^{5}) = 0.12$$



# Heterogeneous Equilibrium



### Heterogeneous Equilibria

- When all reactants and products are in one phase, the equilibrium is homogeneous.
- If one or more reactants or products are in a different phase, the equilibrium is heterogeneous.
- The Heterogeneous Equilibria of solids and liquids are essentially constant
- Both can be obtained by *dividing* the *density* of the substance by its *molar mass* and both of these are constants at constant temperature.

### Heterogeneous Equilibria

- The concentrations of solids and liquids are essentially constant
- We ignore the concentrations of pure liquids and pure solids in equilibrium constant expressions.

$$PbCl_{2(s)} = Pb^{2+}_{(aq)} + 2 Cl_{(aq)}$$

$$K_c = [Pb^{2+}] [Cl^{-}]^2$$



## Equilibrium Calculations



## **Equilibrium Calculations**

- To solve such a problem, use the following procedure
  - Write initial and equilibrium concentrations (or partial pressures) given.
  - Calculate the change in concentration.
  - Use stoichiometry on the change in concentration line only to calculate the changes in concentration of all species.
  - calculate the equilibrium concentrations.



### **Predicting the Direction of Reaction**

• We define Q, for a general reaction

$$a\mathbf{A} + b\mathbf{B}(g) \Longrightarrow p\mathbf{P} + q\mathbf{Q}$$
  
 $\int \mathbf{p} \left[ p \right] p \left[ p \right] q$ 

$$Q = \frac{[\mathbf{P}]^p [\mathbf{Q}]^q}{[\mathbf{A}]^q [\mathbf{B}]^b}$$

where [A], [B], [P], and [Q] are molarities at any time.

• Q = K only at equilibrium.

If Q = K,

### the system is at equilibrium.





### If Q > K, there is too much product and the equilibrium shifts to the left.





### If Q < K, there is too much reactant, and the equilibrium shifts to the right.





### **Applications of Equilibrium Constants** Problem

The following reaction has an equilibrium constant  $K_c$  of 3.07 x 10<sup>-4</sup> at 24°C:

 $2\text{NOBr}(g) \Leftrightarrow 2\text{NO}(g) + \text{Br}_2(g)$ 

For each of the following compositions, decide whether the reaction is at equilibrium. If not, decide which direction the reaction should go.

(a)  $[NOBr] = 0.0610 \text{ M}, [NO] = 0.0151 \text{ M}, [Br_2] = 0.0108 \text{ M}$ (b)  $[NOBr] = 0.115 \text{ M}, [NO] = 0.0169 \text{ M}, [Br_2] = 0.0142 \text{ M}$ (c)  $[NOBr] = 0.181 \text{ M}, [NO] = 0.0123 \text{ M}, [Br_2] = 0.0201 \text{ M}$ 

Ans.: a.) goes left; b.) equilibrium; c.) goes right

# Le Châtelier's Principle





### Le Châtelier's Principle

"If a system at *equilibrium* is *disturbed* by a change in *temperature*, *pressure*, or the *concentration* of one of the components, the system will *shift* its *equilibrium position* so as to counteract the effect of the disturbance."



• Consider the production of ammonia

 $N_2(g) + 3H_2(g) \Longrightarrow 2NH_3(g)$ 

- As the pressure increases, the amount of ammonia present at equilibrium increases.
- As the temperature decreases, the amount of ammonia at equilibrium increases.



#### **Change in Reactant or Product Concentrations**

• Consider the Haber process

 $N_2(g) + 3H_2(g) \Longrightarrow 2NH_3(g)$ 

- If H<sub>2</sub> is added while the system is at equilibrium, the system must respond to counteract the added H<sub>2</sub> (by Le Châtelier).
- The system must consume the  $H_2$  and produce products until a new equilibrium is established.
- So, [H<sub>2</sub>] and [N<sub>2</sub>] will decrease and [NH<sub>3</sub>] increases.



### **The Haber Process**





- Adding a reactant or product shifts the equilibrium away from the increase.
- Removing a reactant or product shifts the equilibrium towards the decrease.



### Effects of Volume and Pressure Changes

- As volume is decreased pressure increases.
- Le Châtelier's Principle: if pressure is increased the system will shift to counteract the increase.
- That is, the system shifts to remove gases and decrease pressure.
- An increase in pressure favors the direction that has *fewer moles of gas.*
- In a reaction with the same number of product and reactant moles of gas, pressure has no effect.



### **Effect of Temperature Changes**

- The equilibrium constant is temperature dependent.
- For an endothermic reaction,  $\Delta H > 0$  and *heat* can be considered as a *reactant*.
- For an exothermic reaction,  $\Delta H < 0$  and *heat* can be considered as a *product*.
- Adding heat favors away from the increase:
  - if  $\Delta H > 0$ , adding heat --- the forward reaction,
  - if  $\Delta H < 0$ , adding heat --- the reverse reaction.
- Removing heat, favors towards the decrease:
  - if  $\Delta H > 0$ , cooling --- the reverse reaction,
  - if  $\Delta H < 0$ , cooling --- the forward reaction

## Catalysts increase the rate of both the forward *and* reverse reactions.



Reaction pathway

lowers the activation energy barrier decrease the time taken to reach equilibrium.

