

EE372 HW#1

Due Date: 17 Mar. 2014 class time

Consider a water heater system with the following transfer function model:

$$T(s) = \frac{\frac{cal}{f}}{\left(\frac{s\tau}{f} + 1\right)^2} P(s)$$

here:

P : Electrical input power (W)

T : Increase in Temperature (°C)

cal : Calorie equivalent of 1 Joule = 0.2388

f : Flow rate of water = 50 cc/s

τ : System parameter = 350 cc

Assume that the system is initially at rest, that is, all initial conditions are zero.

The input power $P(t)$ is limited and can only be adjusted in the range of 0 to 7000 W.

Using a proper input power function $P(t)$, we would like to reach a steady state value of 25°C at the output as fast as possible. In this regard, we would like to minimize the following cost function:

$$J = \int_0^{100} (T(t) - 25)^2 dt$$

Provide your best J value and corresponding input power function $P(t)$ in either as a formula or as a graph.

Note: For simulation, you may want to use the command "lsim" in Matlab.