

Comparison of ATV and M&E BNR Designs

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MONOD KINETICS

<http://www.ohiowater.org/OTCO/downloads/Presentations/WW%2009/Albert%20Pincince.pdf>

SIX

FIVE EQUATIONS THAT CHANGED THE WORLD

$$F = \frac{GMm}{d^2}$$

Newton and the Universal Law of Gravity

$$P + \rho \frac{v^2}{2} = \text{Constant}$$

Bernoulli and the Law of Hydrodynamic Pressure

$$\nabla E = - \frac{\partial B}{\partial t}$$

Faraday and the Law of Electromagnetic Induction

$$\Delta S_{\text{universe}} > 0$$

Clausius and the Second Law of Thermodynamics

$$E = mc^2$$

Einstein and the Theory of Special Relativity

$$\mu = \mu_m \frac{S}{K_s + S}$$

Monod and the Equation for Bacterial Growth

Monod's equation is

$$\mu = \mu_m \frac{S}{K_s + S}$$

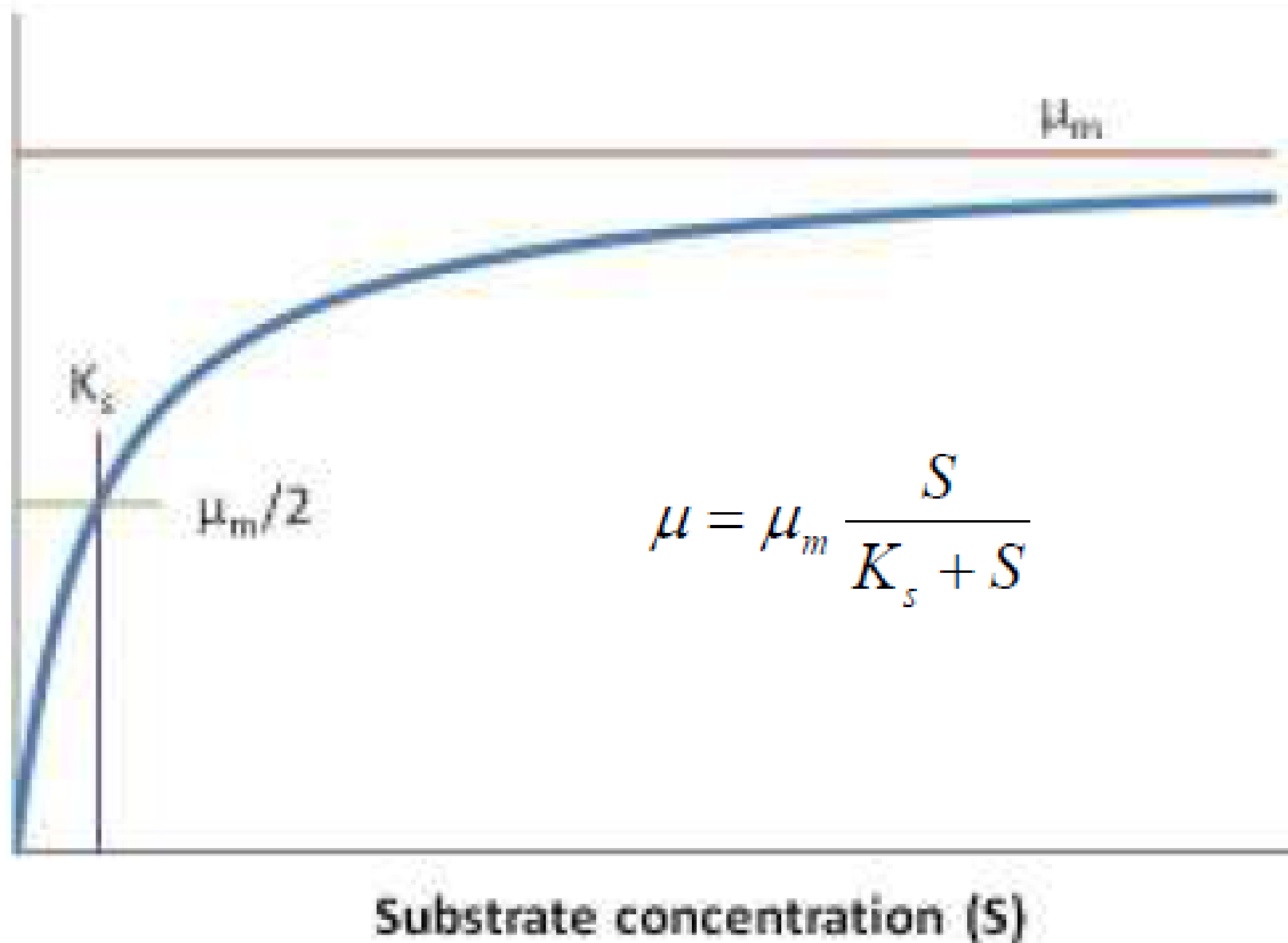
μ = growth rate

μ_m = maximum growth rate

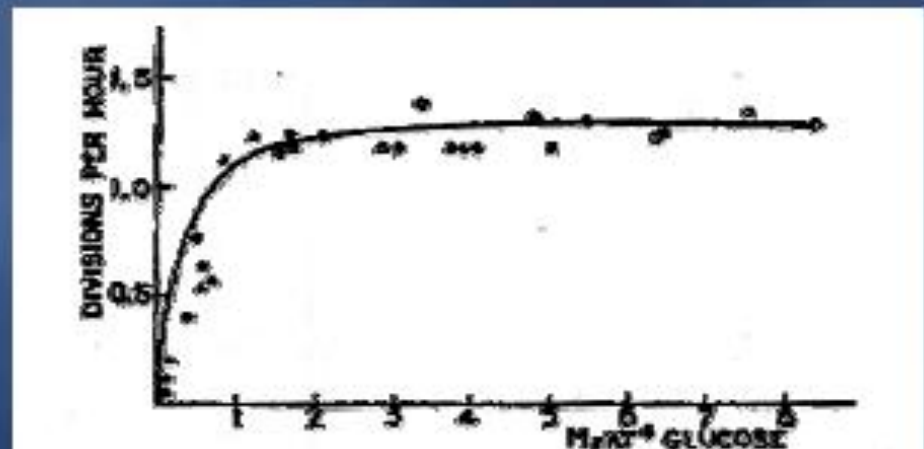
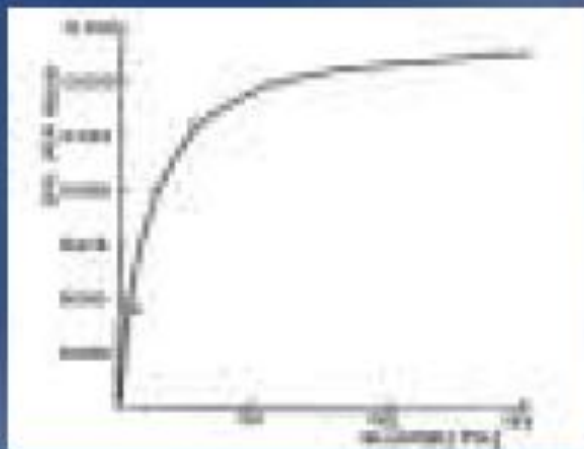
S = concentration of limiting nutrient

K_s = “half-velocity” constant

Growth rate (μ)



- ◆ Not derived from first principles
- ◆ Fit curves to results of batch experiments
- ◆ Equation analogous to one for saturation of hemoglobin
- ◆ Also similar to Michaelis-Menten equation for enzyme kinetics



$$r_g = -Y r_s$$

Herbert and coworkers

- ◆ Developed equations for concentrations of effluent product and of bacteria
- ◆ First used the term “washout”
- ◆ Explained reasons for deviations from theory
 - ◆ Lack of complete mixing
 - ◆ Endogenous respiration—added decay term to equations

$$r_X = (\mu - b)X$$

After Lawrence and McCarty, we end up with these two equations

◆ Equation to determine SRT

$$\frac{1}{\theta_c} = \mu - b$$

where $\mu = \mu_m \frac{S}{K_s + S}$

◆ Equation to determine associated biomass

$$\frac{1}{\theta_c} = Y \frac{F}{M} - b$$

F = mass of BOD **removed**/time
M = volume times concentration

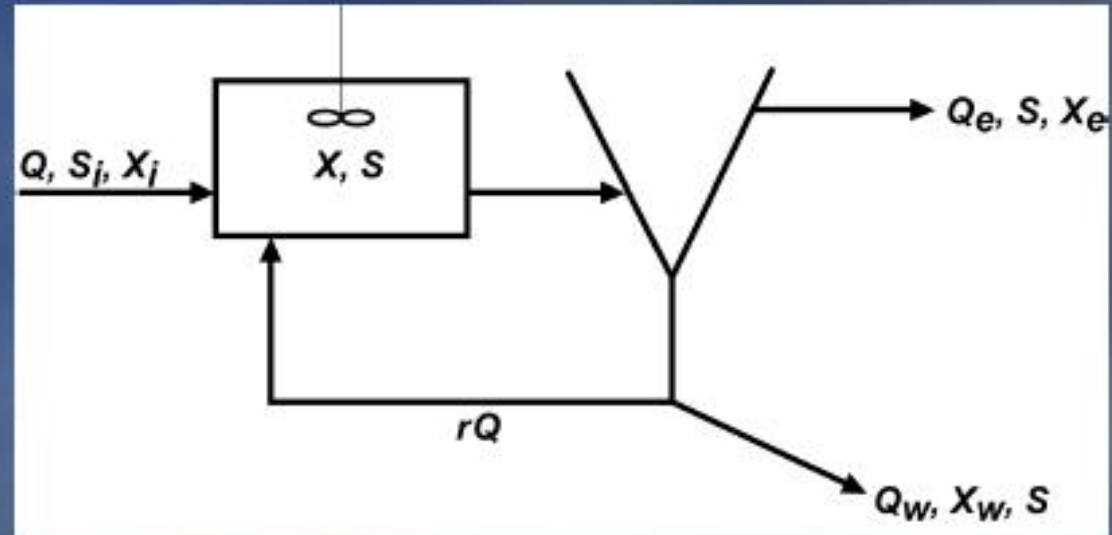
Solids produced are either:

Related to growth:

$$(\mu - b) XV$$

Related to removal of substrate:

$$Y(S_i - S)Q$$



Equations for Mass Balance

Solids in + Solids produced = Solids leaving

Related to growth:

$$QX_i + (\mu - b) XV = Q_e X_e + Q_w X_w$$

Related to removal of substrate:

$$QX_i + Y(S_i - S)Q = Q_e X_e - Q_w X_w$$

Rearranging the two equations:

$$(\mu - b) XV = Q_e X_e + Q_w X_w = P$$

$$Y(S_i - S)Q - bXV = Q_e X_e + Q_w X_w = P$$

**Define mean cell residence time
(or solids retention time or sludge age)
as biomass under aeration divided by
biomass leaving system.**

$$\theta_c = \frac{XV}{Q_e X_e + Q_w X_w} = \frac{XV}{P} = \frac{M}{P}$$

Combine equations

$$\frac{1}{\theta_c} = \mu - b$$

and

$$\frac{1}{\theta_c} = \frac{Y(S_i - S)Q}{XV} - b$$

Introduce F/M Ratio

- ◆ Define F (food) as rate of substrate removal:

$$F = Q(S_i - S)$$

- ◆ Define M as mass in aeration tank

$$M = XV$$

- ◆ Equation based on mass becomes:

$$\frac{1}{\theta_c} = Y \frac{F}{M} - b$$

To determine effluent substrate concentration, look at based on substrate.

$$\frac{1}{\theta_c} = \mu - b$$

◆ **and its equivalent:**

$$\frac{1}{\theta_c} = \mu_{\max} \frac{S}{K_s + S} - b$$

◆ **Rearrange, and solve for S to obtain:**

$$S = \frac{K_s(1 + b\theta_c)}{\theta_c(\mu_{\max} - b) - 1}$$

**To determine biomass in aeration tank,
look at this equation**

$$\frac{1}{\theta_c} = Y \frac{F}{M} - b$$

◆ **and its equivalent:**

$$\frac{1}{\theta_c} = \frac{Y(S_i - S)Q}{XV} - b$$

◆ **Solve for M :**

$$M = VX = \frac{QY(S_i - S)\theta_c}{1 + b\theta_c}$$

**To determine biomass in aeration tank,
look at this equation**

$$\frac{1}{\theta_c} = Y \frac{F}{M} - b$$

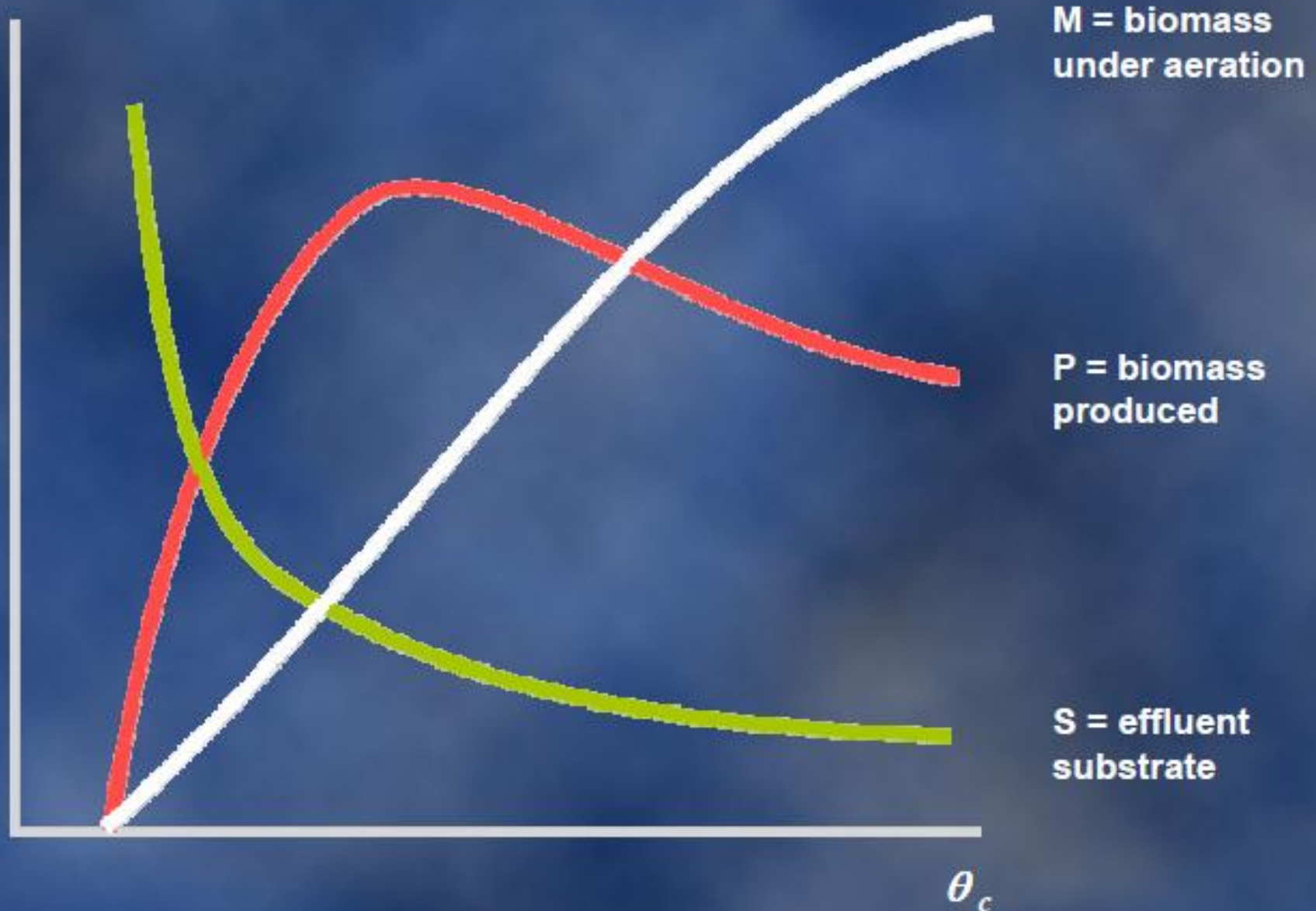
◆ **and its equivalent:**

$$\frac{1}{\theta_c} = \frac{Y(S_i - S)Q}{XV} - b$$

◆ **Solve for M :**

$$M = VX = \frac{QY(S_i - S)\theta_c}{1 + b\theta_c}$$

Plots of equations



When does washout occur?

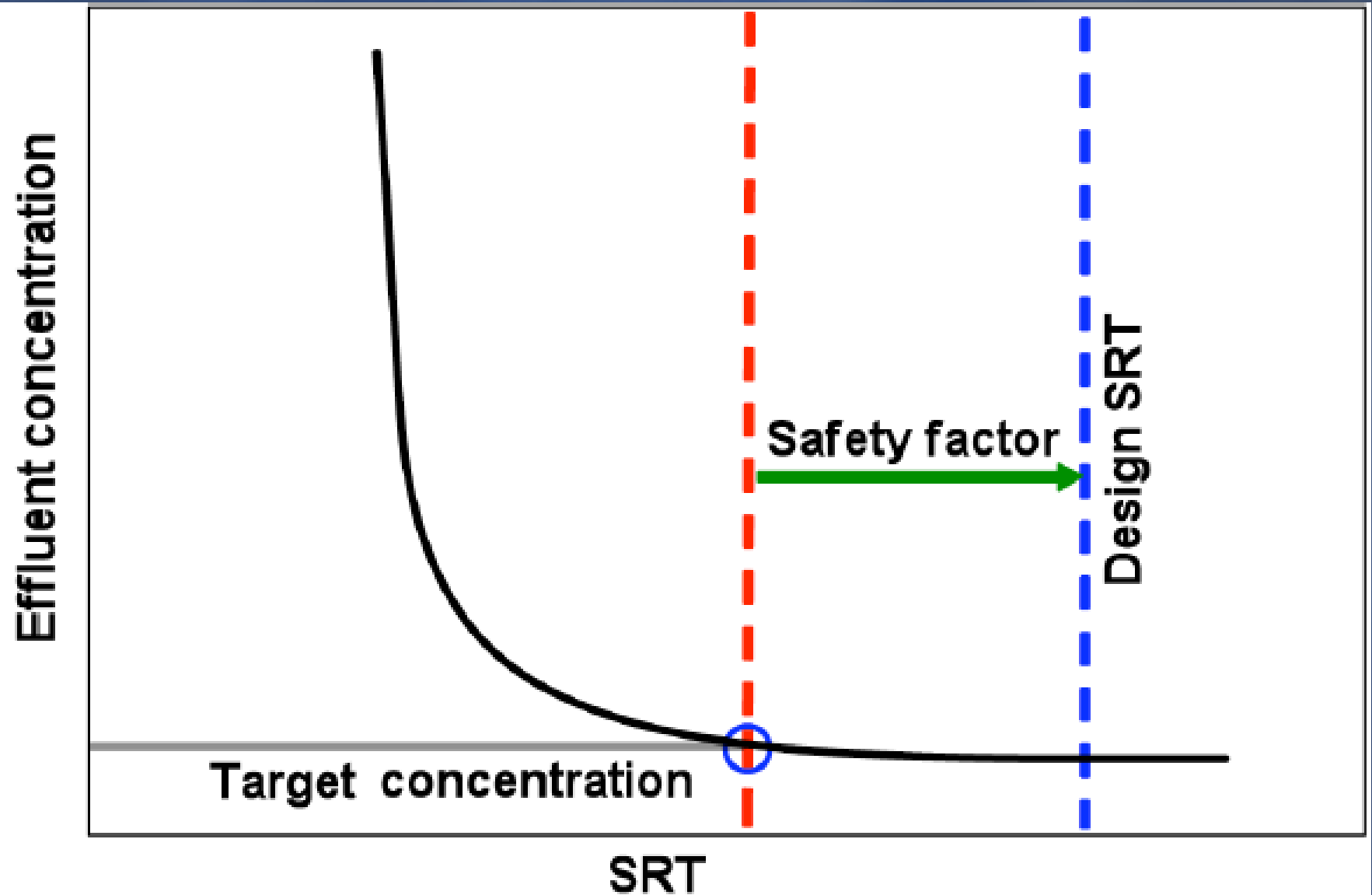
- ◆ At washout, effluent concentration is the same as influent and is much higher than K_s
- ◆ In equation

$$\frac{1}{\theta_c} = \mu_{\max} \frac{S}{K_s + S} - b$$

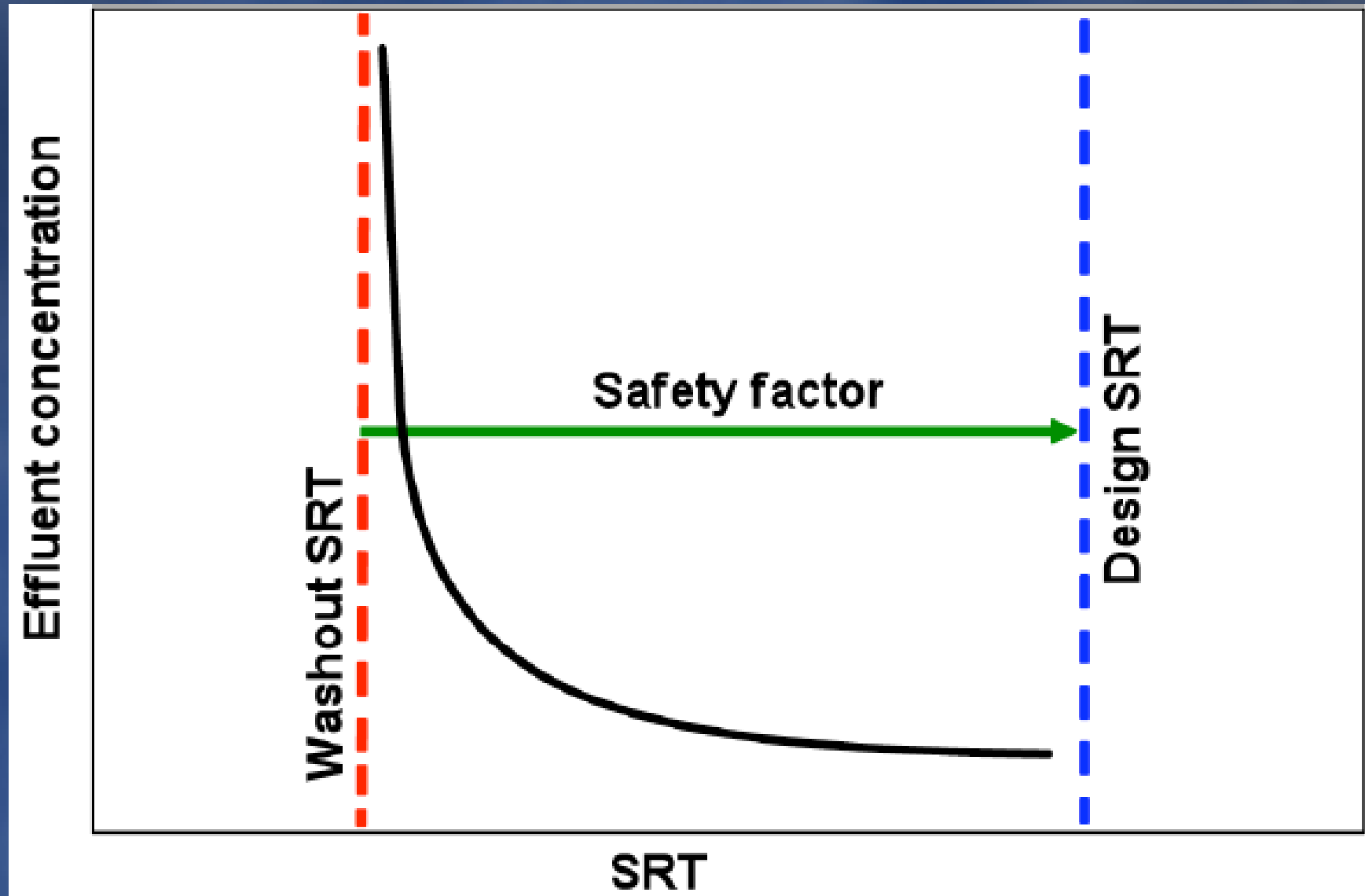
- ◆ K_s is neglected
- ◆ Equation becomes

$$\frac{1}{\theta_c^M} = \mu_{\max} - b$$

Application of safety factor to effluent concentration

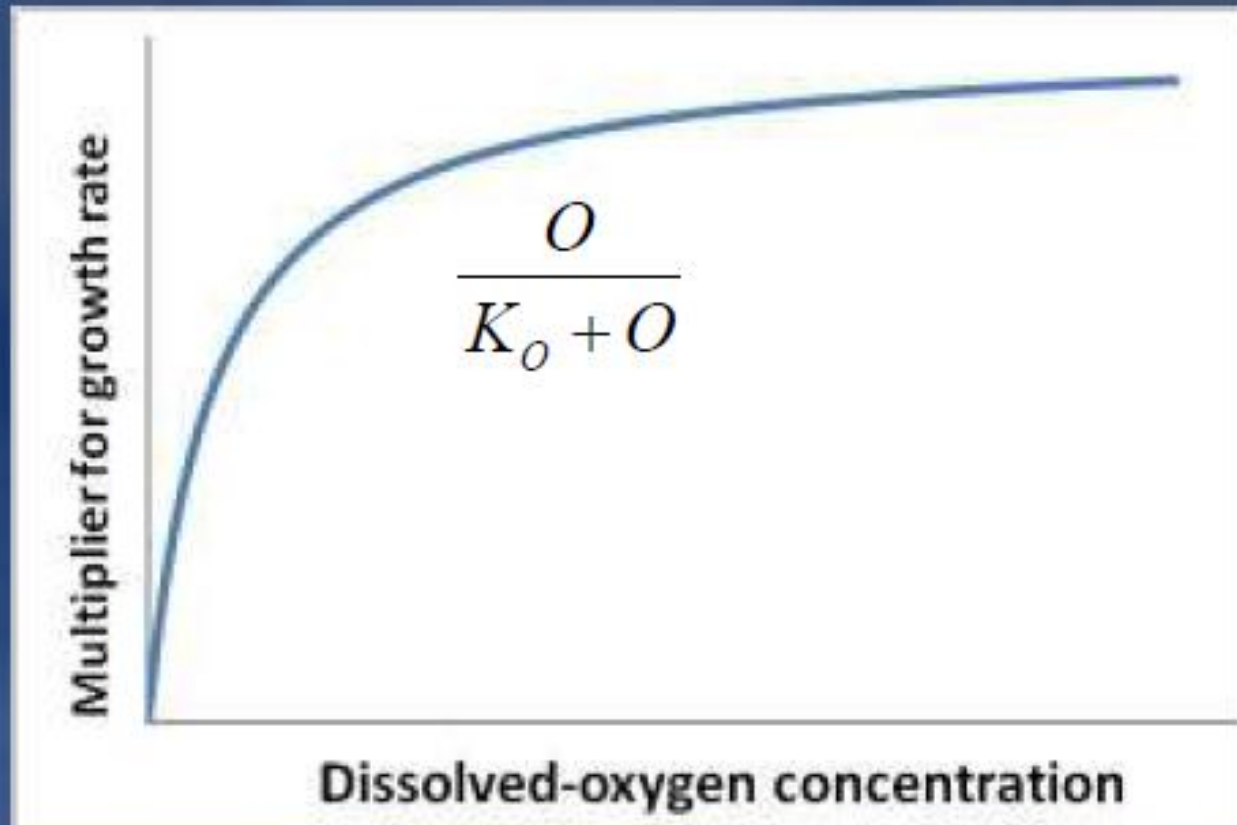


Application of safety factor to washout SRT



Other uses of Monod-type kinetics (I)

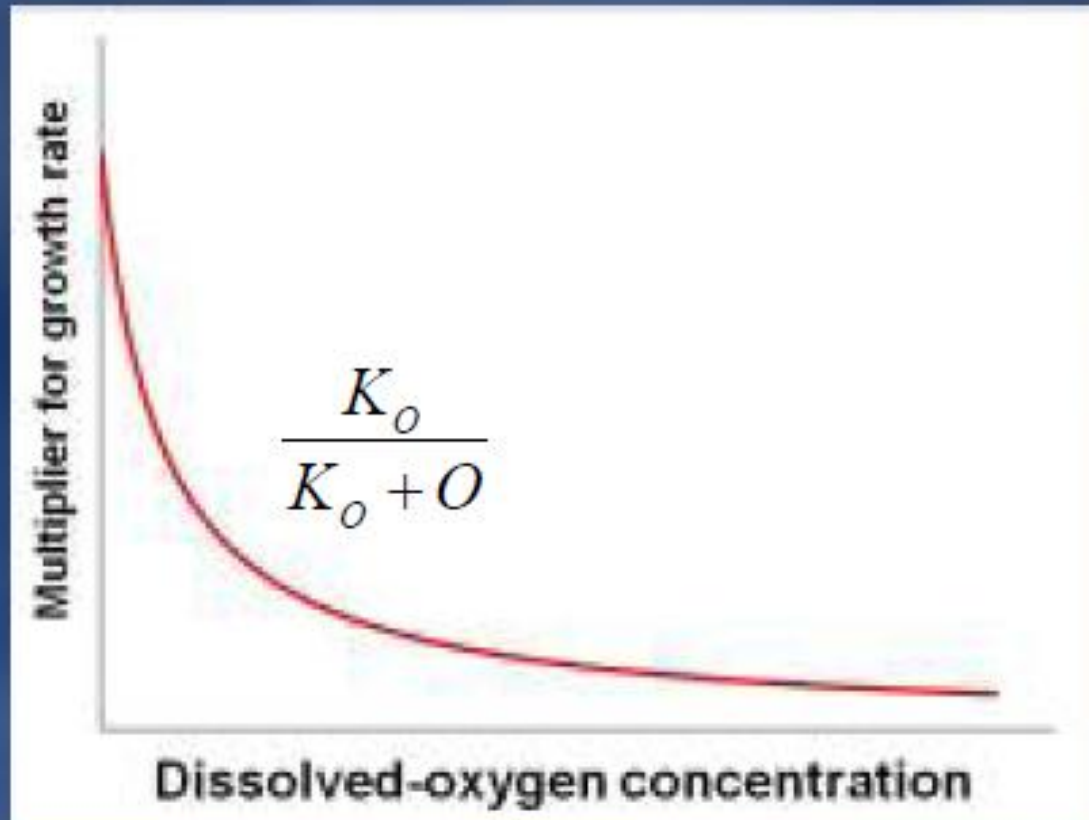
Effect of dissolved-oxygen concentration for aerobic systems



$$\mu = \mu_m \frac{S}{K_s + S} \frac{O}{K_o + O}$$

Other uses of Monod-type kinetics (II)

Effect of dissolved-oxygen concentration for anoxic systems



$$\mu = \mu_m \frac{S}{K_s + S} \frac{K_o}{K_o + O}$$

Other uses of Monod-type kinetics (V)

Examining inhibition

- ◆ Haldane/Andrews

$$\frac{S}{S + K_S + \frac{S^2}{K_I}}$$

- ◆ Competitive

$$\frac{S}{S + K_S \left(1 + \frac{I}{K_I} \right)}$$

- ◆ Noncompetitive

$$\frac{S}{(S + K_S) \left(1 + \frac{I}{K_I} \right)}$$

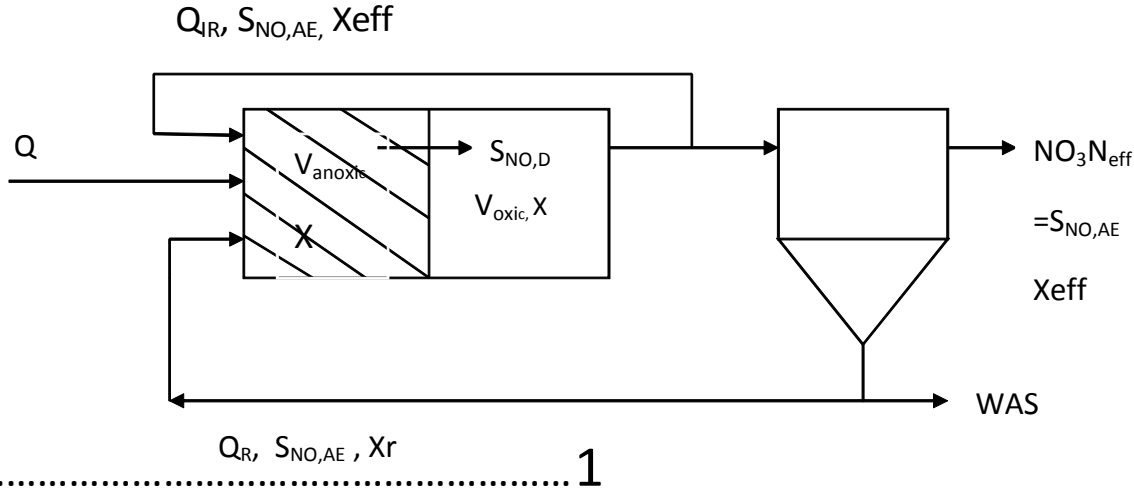
Derivation of:

$$\frac{1}{F / M} = \frac{Y_H SRT}{1 + b_{H,T} SRT}$$

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Rate of substrate utilization:

$$r_{su} = \frac{\mu_H}{Y_H} X_{BH} = -\frac{Q(S_0 - S)}{\forall_T}$$



$$r_g = \mu_H X_{BH} - b_{H,T} X_{BH} = Y_H r_{su} - b_{H,T} X_{BH} \dots\dots\dots 2$$

Making a microorganism mass balance for a completely mixed flow reactor with recycle:

$$\forall_T \frac{dX_{eff}}{dt} = Q_{in} X_{in} - (Q_W X_{BH} + Q_{eff} X_e) - \forall_T r_g \dots\dots\dots 3$$

At steady-state, and for $X_{in}=0$, substituting r_g from Eq 2 in Eq3;

$$\frac{Q_w X_{BH} + Q_{eff} X_e}{\forall_T X_{BH}} = Y_H \frac{r_{su}}{X_{BH}} - b_{H,T} \dots\dots\dots 4$$

$$\frac{1}{SRT} = Y_H \frac{r_{su}}{X_{BH}} - b_{H,T} \dots\dots\dots 5$$

Substituting r_{su} from Eq1;

$$X_{BH} = -\frac{Q(S_0 - S)}{\forall_T} * \frac{Y_H SRT}{1 + b_{H,T} SRT} \dots\dots\dots 6$$

$$\frac{1}{F/M} = -\frac{\forall_T X_{BH}}{Q(S_0 - S)} = \frac{Y_H SRT}{1 + b_{H,T} SRT} \dots\dots\dots 7$$

From definiton of SRT;

$$P_{X,T} = \frac{\forall_T X}{SRT} = \frac{Y_H Q(S_0 - S)}{(1 + b_{H,T} SRT)}$$

Dependence of $S_{\text{NO}_3\text{Neff}}$ on Internal Recirculation (IR)

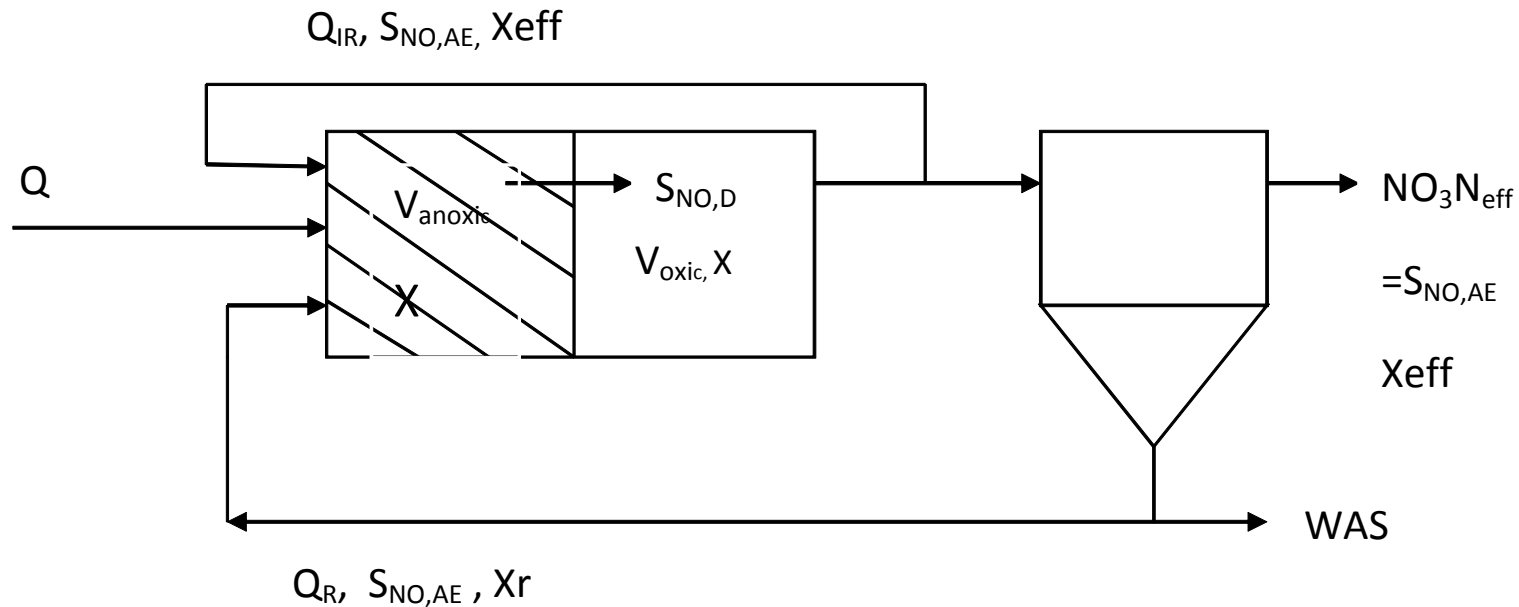
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Derivation of Dependence of $S_{NO_3N_{eff}}$ on Internal Recirculation (IR)

$$TN_{in} = TKN_{in} + NO_3N_{in}$$

$$\text{Assume } NO_3N_{in} = 0$$

$$\text{TKN nitrogen to be oxidized} = (TN_{in} - TKN_{eff}) - X_{orgN,WAS} = (1 + R + IR)(S_{NO,AE} - S_{NO,D})$$



$$IR = \frac{(TKN_{in} - TKN_{eff} - X_{orgN,WAS})}{S_{NO,AE} - S_{NO,D}} - (1 + R)$$

$$IR = \frac{(TKN_{in} - TKN_{eff} - X_{orgN,WAS})}{S_{NO,AE} - S_{NO,D}} - (1 + R)$$

Assume optimized anoxic volume and $S_{NO,D}=0$

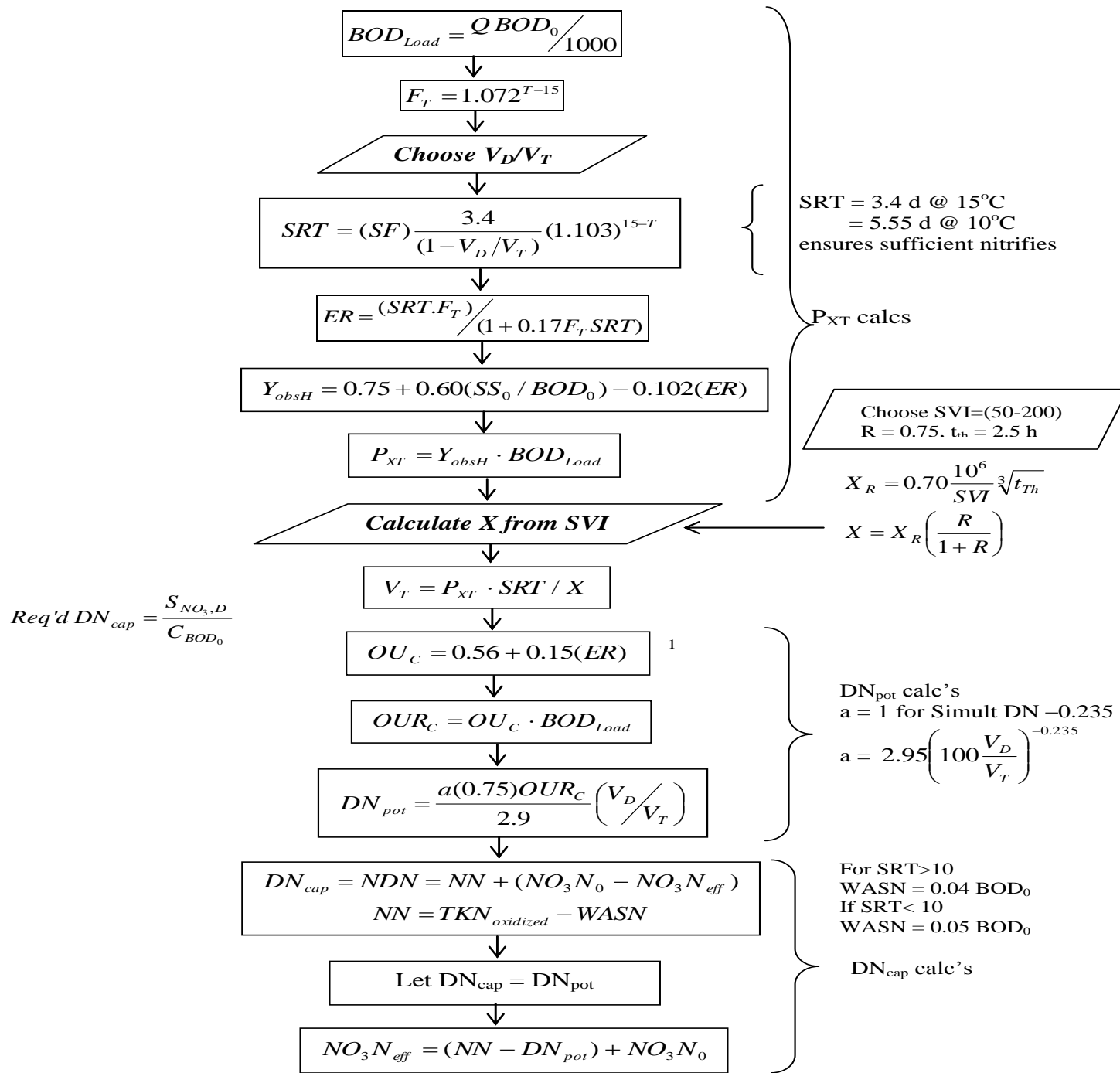
$$IR = \frac{NO_x}{NO_3N_{eff}} - (1 + R)$$

Nitrate to be denitrified = $Q(R+IR)*NO_3N_{eff}$

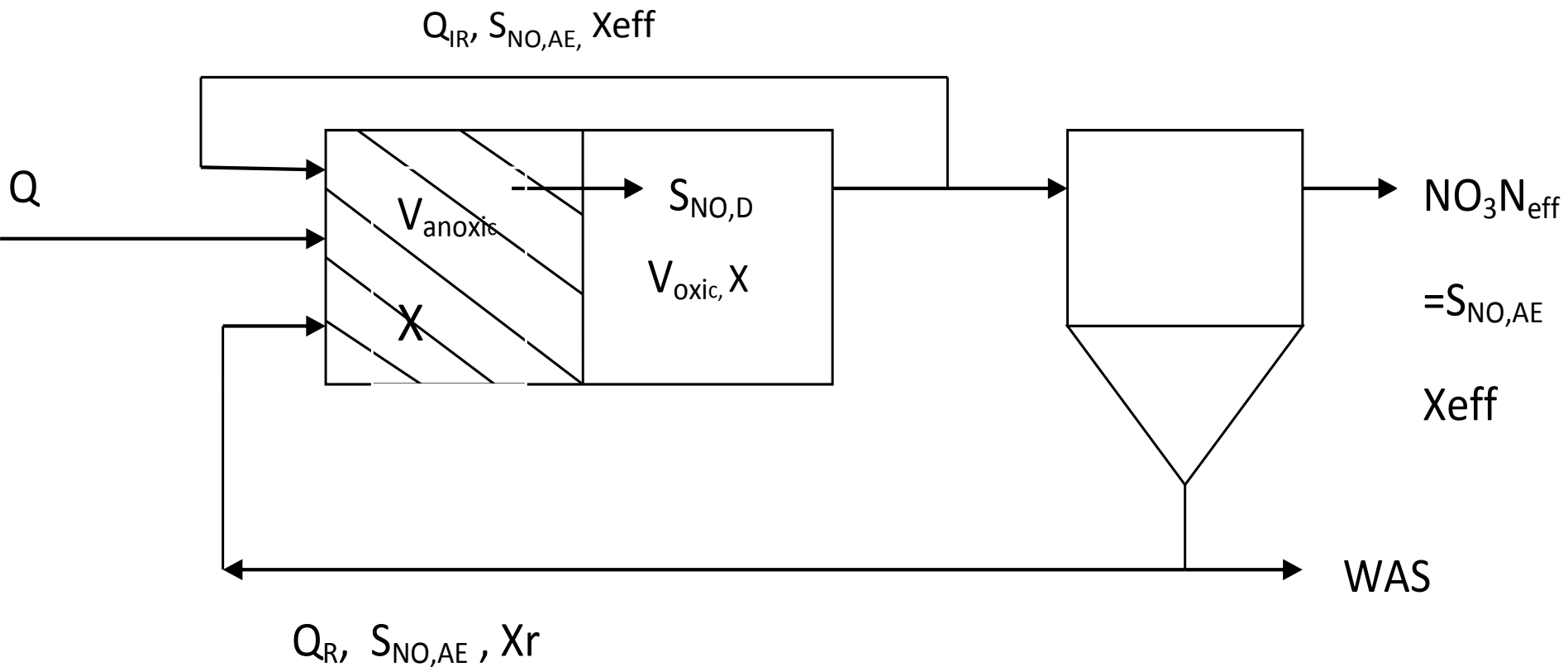
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ATV in a Nutshell



S & X Mass Balances in Pre-DN



A. Calculating Aerobic Sludge Age (SRT_a)

Writing in terms of ASM Model Notations

$$\mu_A = \hat{\mu}_A = \left(\frac{S_{NH}}{K_{NH} + S_{NH}} \right) \left(\frac{S_0}{K_{0,n} + S_0} \right) - b_A$$

$$\hat{\mu}_{A,T} = \mu_{A,20} (1.07)^{T-20}$$

$$SRT_a = \frac{1}{\mu_{A,T} * SF}$$

A. Biological Sludge Production ($P_{x,bio}$)

Effluent BOD Concentrations, S :

$$S = K_s \frac{(1 + b_{H,T} SRT_a)}{SRT_a (\mu_{H,T} - b_{H,T}) - 1}$$

$$b_{H,T} = b_{H,20} (1.04)^{T-20}$$

$$\mu_{H,T} = \mu_{H,20} (1.07)^{T-20}$$

$$P_{x,bio} = \underbrace{QY_H \frac{(S_0 - S)}{1 + b_{H,T} SRT_a}}_{P_{X,H}} + \underbrace{QY_H f_d b_{H,T} \frac{SRT_a (S_0 - S)}{1 + b_{H,T} SRT_a}}_{\substack{P_X\text{-particulates} \\ \text{formed from decay} \\ \text{of heterotrophs}}} + \underbrace{QY_A \frac{NO_X}{(1 + b_{A,T} SRT_a)}}_{P_{X,A}}$$

$$NO_X = \text{Oxidized TKN} = \underbrace{TKN_{in} - TKN_{eff}}_{TKN_{oxid}} - \underbrace{0.12(P_{x,bio}/Q)}_{X_{orgN,WAS}}$$

A. Total Sludge Production ($P_{X,TSS}$)

$$P_{X,TSS} = \frac{P_{X,bio}}{0.85} + Q \cdot nbVSS + Q(TSS_0 - VSS_0)$$

$$\frac{MLVSS}{MLSS} = \frac{P_{X,VSS}}{P_{X,TSS}}$$

$$nbVSS = \left(1 - \frac{bpCOD}{pCOD}\right)VSS$$

$$VSS_0 = 0.65TSS_0$$

$$bpCOD = 27\%$$

$$pCOD = 40\%$$

Choose X_T

$$\forall_a = \frac{(P_{X,TSS} + P_{X,PO_4})}{X_T} SRT_a$$

$$X_R = 2X \quad \left\{ \quad \frac{X}{X_R} = \frac{R}{1+R}, R = 1 \right.$$

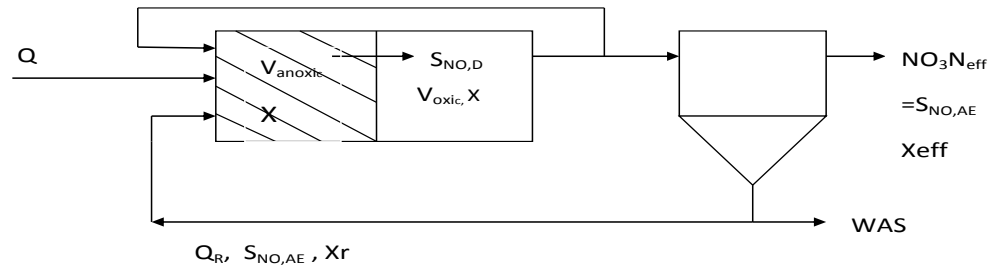
$$IR = \frac{NO_X}{S_{NO_3 N_{eff}}} - (1 + R)$$

$$SDNR_{20} = 0.19 \frac{gNO_3 N / d}{gMLVSS}$$

$$SDNR_T = SDNR_{20} (1.026)^{T-20}$$

$$\frac{1}{(F / M)_a} = \frac{\forall_a \cdot MLVSS_{biomass}}{Q(S_0 - S)} = Y_H \frac{SRT_a}{1 + b_{H,T} SRT_a}$$

$$MLVSS_{biomass} = \frac{Y_H SRT_a Q(S_0 - S)}{\forall_a (1 + b_{H,T} SRT_a)}$$



Total NO_3N recirculated is denitrified.

$$\text{Required } \text{NO}_3\text{N removal} = Q(R+IR) \cdot \text{NO}_3\text{N}_{\text{eff}}$$

Assume a retention time for anoxic tank, $t_{R,DN}$

$$\forall_{DN} = \frac{Q}{24} * t_{R,DN}$$

$$\text{NO}_3\text{N removed} = \forall_{DN} * \text{SNDR}_T * \text{MLVSS}_{\text{biomass}}$$

$$\forall_T = \forall_{DN} + \forall_a$$

$$\text{SRT}_T = \frac{X_T * \forall_T}{P_{X,TSS}}$$